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A Regional Model for the Portuguese Economy Based on a Regional Accounting Matrix

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resumo

résumé / abstract

Este artigo apresenta um modelo para a economia portuguesa assente numa "Matriz de Contabilidade Regional" (MCR). A MCR é um quadro contabilístico, construído a partir de Contas Nacionais e Regionais oficiais, com uma estrutura inspirada nas matrizes de contabilidade social, em que as regiões assumem o papel aí desempenhado pelos grupos sociais. Partindo da MCR, o artigo desenvolve um modelo tipo input-output, fechado em relação ao consumo das famílias. Este modelo baseia-se numa "hipótese de inexistência de preferência regional na satisfação da procura". O modelo permite o cálculo de diversos multiplicadores, salientando-se os que descrevem o processo de distribuição inter-regional do rendimento. Com efeito, um aumento de rendimento, numa primeira fase em benefício das famílias de uma região, pode cruzar as fronteiras regionais, e propagar-se a outras regiões, aumentando o rendimento das famílias aí residentes.

Cet article présente un modèle pour l'économie portugaise reposant sur une "Matrice de Comptabilité Régionale" (MCR). La MCR est un tableau comptable, élaboré à partir de Comptes Nationaux et Régionaux officiels, dont la structure s'inspire des matrices de comptabilité sociale, tableau dans lequel les régions assument le rôle joué par les groupes sociaux. A partir de la MCR, l'article développe un modèle du type input-output, fermé en ce qui concerne la consommation des familles. Ce modèle se base sur une "hypothèse d'inexistence de préférence régionale dans la satisfaction de la demande". Le modèle permet le calcul de divers multiplicateurs, mettant en évidence ceux qui décrivent le processus de distribution interrégionale du revenu. En effet, une augmentation de revenu, dans une première phase au profit des familles d'une région, peut se faire croiser les frontières régionales et s'étendre à d'autres régions, augmentant ainsi le revenu des familles qui y résident.

This paper presents a model for the Portuguese economy based on a so-called "Regional Accounting Matrix" (RAM). The RAM is an accounting table made up of information provided by the standard National and Regional Accounts, with a framework inspired in the social accounting matrixes, where regions took the place of the social groups. Starting with the RAM, the paper then develops an input-output-type model closed with respect to the households' consumption. This model is based on a "hypothesis of nonexistence of regional preference in supplying regions". The model allows the computation of several multipliers – the most striking of them describe the inter-regional income distribution process. In fact, an increase in income, at the beginning in benefit of the households living in one region, may cross the region borders and propagate into other regions, increasing then the households' income in the latter regions.

1. Introduction* 1



This paper presents a model for the Portuguese economy based on a so-called "Regional Accounting Matrix" (RAM). The proposed RAM, which regards the year of 1995, is an accounting table made up of information provided by the standard Portuguese National and Regional Accounts, with a framework inspired in the social accounting matrixes², where regions took the place of the social groups. As in a social accounting matrix, the RAM is the outcome of an incision of complementary information into a common National Accounts framework. In the case of the RAM that complementary information is mainly based on Regional Accounts, being the use of other sources, beyond those from National and Regional Accounts, confined to very exceptional cases. Starting with the RAM, the paper then develops an input-output-type model that allows the inferring of some interesting results at regional level: the most striking of them aim to describe the inter-regional households' income distribution process.

The peculiarity of the RAM³ – and of the input-output model derived from it – that we are going to unfold, is that they mingle information at national level with other that is known at regional level. Indeed, the regionalised data are confined to the households' generation and use of income. As to other components of final demand, as the GFCF or the international exports, only national totals are considered. The inter-industry relationships are at national level as well. In fact, concerning the production process, we know the place where the Gross Value Added is generated – and distributed to the households – but the technological information, i. e., the structure of inputs of the intermediate consumption is not available by regions. This unusual mix of regional and national information led to a model that works under a crucial assumption that we designate as the "hypothesis of non-existence of regional preference in supplying regions". By that hypothesis we mean:

• that every increase in demand, even when regionally located, is matched by a national supply (and also by international imports), and not preferentially by an increase in output of the very concerned region; this national supply is provided by regions, and by the rest of the world, in fixed proportions that do not depend on the region where the demand emerged.

Though this is an infrequent assumption on regional input-output models, where otherwise it is much more common to assume that imports are exogenous and thus increases in demand command regional adjustments in supply, we do believe that it is a reasonable idea for Portugal. In fact, Portugal is a small country with reduced distances, both in time and cost, benefiting of well-integrated markets, with diffuse borders between regions over which economic effects easily spread. Please remark that although we are arguing that this is a suitable hypothesis for a country as Portugal, we do not pretend that it is the best assumption. Indeed, it is the necessary hypothesis under which our model – that uses a limited set of available information – does work.

^{*} The author gratefully acknowledges the comments and suggestions of two anonymous referees of this journal. The usual disclaimer applies.

¹ The theoretical structure of the Regional Accounting Matrix (RAM) that we develop in this paper was presented once in a meeting of the APDR (the Portuguese Regional Development Association) that took place in Ponta Delgada, Azores, in July 2000 (Ramos, 2000). An early version of this article, including the application to the Portuguese economy, was presented at the 41st ERSA congress in Zagreb, Croatia (Ramos, 2001).

² On social accounting matrixes see, for instance, Lager (1998) and Pyatt and Round (1998). Our model can also be seen as proceeding from the Miyazawa's models developed in the sixties and seventies, some of them reproduced and/or shortened in Miyazawa (1976). However, the regional model proposed by Miyazawa (1976), in his chapter 2, assumes a more extensive set of regional information than ours, thus avoiding an assumption such as our "hypothesis of non-existence of regional preference in supplying regions".

³ We did not attach to this paper the RAM that we produced for the Portuguese economy because of its considerable size. However, the RAM (and the inverted matrices that we derived from that original table) can be provided under request through the e-mail address: pnramos@fe.uc.pt



The remaining of this paper is organised as follows: in section 2 we explain the framework that we adopted in building up the Portuguese RAM; section 3 is devoted to the input-output-type model that is associated to the RAM - the meaning of the main multipliers that are produced by that model is explained there; section 4 concludes presenting the most outstanding results that we obtained for Portugal. The paper encloses an annex where the procedure used for inverting the input-output matrix is summarised.

2. The framework of the Regional Accounting Matrix

Matrix A below depicts the structure of a RAM as we performed it for the Portuguese economy, where the \mathbf{A}_{ij} are sub-matrices and the \mathbf{q}_i , \mathbf{q}'_i , \mathbf{s}_3 and \mathbf{t}'_3 are vectors calculated by adding up the rows and the columns of A (in this paper, capital letters designate matrices and small letters vectors).

(1)
$$A = \begin{bmatrix} A_{11} & A_{12} & A_{13} & q_1 \\ \hline A_{21} & A_{22} & A_{23} & q_2 \\ \hline A_{31} & A_{32} & 0 & s_3 \\ \hline q'_1 & q'_2 & t'_3 \end{bmatrix}$$

 A₁₁ is an inter-industry table with 49 rows and 49 columns, of the input-output type, compiled at national level, where each entry represents the sales of one commodity to be used in the production process of one industry; this matrix is provided by the National Accounts, but the VAT that is borne by the intermediate consumption is excluded from its cells

 ${f A}_{12},\,{f A}_{21},\,{f A}_{22},\,{f A}_{32}$ and ${f A}_{23}$ altogether form the households' accounts that are disaggregated by the 7 Portuguese regions according to the location of the residence of those households.

- $-A_{12}$ is a 49 x 7 sub-matrix embracing the private consumption of the households, by commodities and by regions; in a first step we split the consumption by regions taking into account the households regional disposable income known through the official Regional Accounts, and an estimation of the regional average propensities to consume; these regional propensities were themselves averages of primary estimates obtained through three different methodologies: the propensities implicit in the Survey on Households' Budgets 1995, elaborated by the Portuguese Statistical National Institute (INE); those deriving from another study by INE relating to regional purchasing power (INE, 1997); and finally the results of assuming that the saving structure by regions is equal to the regional structure of private deposit interests; in a second stage, we decomposed households' consumption in each region by commodities, using the information contained in the Survey on Households' Budgets 1995 4;
- A21 is a 7 x 49 matrix that describes the generation of income in each one of 49 industries that benefits the households residing in the seven regions; that income includes the compensation of employees residing in the regions and the operating surplus appropriated by the own-account workers that are classified in the households' institutional sector (the additional information for splitting the operating surplus by sectors was provided by the National Accounts);

⁴ The outcome of this two-stages process is a structure of the national private consumption, by commodities, that is different from the one that is taken in the National Accounts. The difference between the two estimates is a vector of "errors" that was transferred to A₁₃. This vector also includes the consumption of non-residents on the national territory (minus the consumption of residents made abroad) and the consumption of the households that are deemed to be resident in the Extra-regio. The Extra-regio is the part of the economic territory which cannot be attached directly to a single region, for instance embassies or consulates (Eurostat, 1996, 13.06).

— A₂₂ is a transfer matrix (7 x 7) where we record some flows that redistribute households' income among regions (we only consider here the income of the landlords that live in a region different from the one where their estates are located, other cases being neglected; as a matter of fact, only transfers corresponding to estates located in Alentejo were deemed to be relevant);



- A_{32} refers to other uses of the households' income as income taxes, social contributions, other transfers to other institutional sectors, and of course saving, all these flows being computed at regional level
- ${\bf A_{23}}$, at last, includes other sources of households' income, namely compensations received from abroad, property income (dividends, interests, etc.), social benefits, and other transfers from the other institutional sectors or from the rest of the world to the households residing in different regions.
- ${\bf A_{31}}$ and ${\bf A_{13}}$ are the constituent parts of the total supply and demand of the outputs that are resources or uses of other institutional sectors but households. The matrix ${\bf A_{31}}$ comprises the factor incomes benefiting other institutional sectors, as the operating surplus not directly appropriated by the households, the compensation of employees residing abroad, and taxes on production less subsidies (including the VAT that fall upon intermediate and final consumption). It also includes international imports, taxes and duties on these imports, trade margins, and a row concerning by-products and incidental sales of some branches of activity that allows to transform industry outputs into commodity outputs⁵. ${\bf A_{13}}$ that joins the products final demand but the regionalised households consumption, is mainly composed by the investment, the collective consumption and the international exports columns, as well as the intermediate demand corresponding to the imputed production of the banking sector. Matrices ${\bf A_{31}}$ and ${\bf A_{13}}$ are not regionalised.

The column-vector \mathbf{q}_1 and its transposed row-vector $\mathbf{q'}_1$ measure the total demand and supply (which are of course equal) of the 49 groups of commodities. In the same way, \mathbf{q}_2 and $\mathbf{q'}_2$ represent the total flows of generation and use of the households' income. On the other hand, \mathbf{s}_3 and $\mathbf{t'}_3$ are respectively the total resources and the total uses of the other institutional sectors (as a matter of fact \mathbf{s}_3 includes the households' saving and $\mathbf{t'}_3$ its application through the households' capital accounts). We do not assume $\mathbf{s}_3 = \mathbf{t}_3$, we only enforce $\mathbf{i's}_3 = \mathbf{i't}_3$ where $\mathbf{i'}$ is a row-vector fulfilled with $1s^6$.

3. The input-output model based on the RAM

Turning the RAM structure, which we described in the previous section, into an input-output model essentially requires that we decide which part of A is exogenous and which one includes the endogenous entries. Our assumption, in this section, is that \mathbf{A}_{11} , \mathbf{A}_{21} , \mathbf{A}_{12} and \mathbf{A}_{22} are the endogenous ones, depending on the total outputs of the 49 commodities \mathbf{q}_1 and on the 7 regional total incomes of the households \mathbf{q}_2 :

(2)
$$A_{11} = A^*_{11} \cdot \hat{Q}_1$$

$$A_{21} = A^*_{21} \cdot \hat{Q}_1$$

$$A_{12} = A^*_{12} \cdot \hat{Q}_2$$

$$A_{22} = A^*_{22} \cdot \hat{Q}_2$$

⁵ Note that the proposed RAM is still based on National and Regional Accounts that follow the 1979 European System of Accounts. That explains some peculiarities in the way we dealt with by-products and incidental sales. For more details in the process of turning industries into commodities, please see the Annex to this paper. 6 It could also be assumed $\mathbf{s}_3 = \mathbf{t}_3$. However, this would require that \mathbf{A}_{31} , \mathbf{A}_{32} , \mathbf{A}_{13} and \mathbf{A}_{23} were organised by institutional sectors and not by kind of transaction. Nevertheless, this alternative and more intricate shape of the RAM did not seem, in our opinion, to be worthwhile.



 A_{11}^* , A_{21}^* , A_{12}^* and A_{22}^* are technical coefficients matrices and \hat{Q}_1 and \hat{Q}_2 are diagonal matrices whose main diagonals share the entries of q_1 and q_2 . Because A_{21} , A_{12} and A_{22} are assumed to be endogenous, our model is stated to be closed with respect to the private consumption.

Under these assumptions we can write:

(3')
$$A^* \cdot q + A_3 i = q \Leftrightarrow A^* \cdot q + e = q^7$$

where $\mathbf{e} = \mathbf{A_3} \mathbf{i}$ (i is a vector of 1s) means the exogenous demand and income vector obtained by adding up the columns of $\mathbf{A_3}$. This vector is composed of two parts: $\mathbf{A_{13}} \mathbf{i}$, which is the exogenous final demand excluding private consumption; and $\mathbf{A_{23}} \mathbf{i}$, where is recorded the exogenous income of the households residing in the 7 regions that is not proceeding from their production activity. Solving the matricial equation (3'), we have:

(4)
$$(I - A^*) \cdot q = e \Rightarrow (5) q = (I - A^*)^{-1} \cdot e$$

Matrix ($\mathbf{I} - \mathbf{A}^*$)-1 in (5), which we designate as \mathbf{B} as well, computes the impacts of the increases in the entries of \mathbf{e} – that is to say in exogenous final demand and in exogenous income – over the entries of \mathbf{q} , i. e. over the commodities' output or the total income of the households residing in the seven regions. Matrix \mathbf{B} is therefore the (accountants) multipliers' matrix that we can split in four sub-matrices:

(6)
$$B = \begin{bmatrix} B_{11} & B_{12} \\ B_{21} & B_{22} \end{bmatrix}$$

$$A^* g + e = q$$
 (the equation (7) of the Annex)

However, as \mathbf{g} can be written as a function of \mathbf{q} , we can reach an equation of the type of (3') above. Please, see the Annex for more details in this procedure.

⁷ In the main text of this article we did not emphasize the difference between commodity supplies (the vector \mathbf{q}_1) and industry outputs (that are part of the vector \mathbf{g} of the Annex). That difference happens because some commodities are produced as secondary production (by-products/incidental sales) in several industries. As a matter of fact, in our calculation technical coefficients are settled dividing intermediate consumptions by industry outputs instead of the commodity supplies included in \mathbf{q}_1 . Thus our starting point is:

in which:



- B_{11} refers to the national multipliers on output, which mean the effects of increasing exogenous final demand on commodity outputs besides the place where they are produced (income induced effects are included)
- B_{21} is a matrix of multipliers describing the impacts on regional households' incomes of changing the final demands of the 49 groups of commodities in any place of the national territory
- B₁₂ brings together the multipliers representing the changes in outputs at national level induced by changes in the households' regional incomes, and
- B₂₂, last but not least, is the matrix of the inter-regional households' income redistribution process, whose multipliers reckon the total impacts on the income of each region of exogenous changes on the income of the other (or the same) regions⁸.

4. Some results for the Portuguese economy

The inter-regional income redistribution analysis allowed by the \mathbf{B}_{22} multipliers is beyond any doubt the most interesting outcome of this study. Our main idea is that regions cannot fully profit from the increases in income that their households benefit in a first wave. On the contrary, changes in income in one region do cross the region borders and propagate into other regions, because those increases in income and then in consumption in the former region imply a growth of the output everywhere, which compel further increases in other regions' income as well. Table 1 shows us those inter-regional income effects for the Portuguese economy; the upper part of the table is matrix \mathbf{B}_{22} .

	Northern Region	Central Region	Lisbon and T. Valley	Alentejo	Algarve	Azores	Madeira
Northern Region	1.1479	0.1388	0.1456	0.1341	0.1600	0.1361	0.1317
Central Region	0.0736	1.0693	0.0720	0.0665	0.0796	0.0682	0.0650
Lisbon and Tagus Valley	0.2052	0.1904	1.2032	0.1877	0.2213	0.1839	0.1784
Alentejo	0.0226	0.0209	0.0221	1.0207	0.0237	0.0211	0.0200
Algarve	0.0212	0.0194	0.0210	0.0193	1.0238	0.0185	0.0182
Azores	0.0099	0.0091	0.0098	0.0091	0.0106	1.0095	0.0089
Madeira	0.0105	0.0097	0.0105	0.0096	0.0117	0.0094	1.0095
Population (10 ³)	3524.9	1712.5	3309.6	526.4	345.1	241.0	257.0
GDP per capita	1409.1	1363.4	2007.1	1316.1	1584.6	1117.6	1241.6

⁸ We can also find an inter-regional income redistribution matrix in Miyazawa (1976), chapter 2. However, as we explained in footnote 2, Miyazawa's underlying model is different, incorporating more information at regional level (for instance we did not regionalise ${\bf A_{11}}$ and then ${\bf B_{11}}$ is not regionalised as well).





The lower part of the table includes the population and the GDP per capita of the Portuguese regions in 1995. Looking at the main diagonal of the matrix, we can conclude that the intra-regional income multipliers are higher in the biggest and in the richest regions: the Northern Region and the Lisbon and Tagus Valley region. The reason why we find right there the most meaningful multipliers is that those regions guarantee the major share of the national output. Hence, indirect effects on output remain inside the regions in a large scale; leakages for other regions are reduced to a minimum. On the other hand, smallest regions as the Alentejo, Algarve or the islands (Azores and Madeira) have a more specialised production apparatus, so income effects are very often rerouted towards other regions where consumption goods are mainly produced.

The very same reasons also explain, if we look at the multipliers located out of the main diagonal, which represent the cross-effects between regions, why increasing income in the smallest and the poorest regions has a more important impact on other regions than the opposite effect. That means that income in Portugal mainly flows from the smallest and poorest regions as Alentejo or the islands into the biggest and richest regions as Lisbon and Tagus Valley or the Northern Region. We should stress, however, that that conclusion concerns only the kind of income effects that are embraced by an input-output-type model, namely the automatic effects on the production income, appropriated by the households, which are induced by a growing consumption.

Regarding the two main Portuguese regions - Northern Region and Lisbon and Tagus Valley, which have a similar size in terms of their population - it is interesting to note that the Lisbon region benefits more in its inter-relationship with the Northern Region than the opposite. That happens in spite of the fact that Northern Region is the main industrial region in Portugal (but its industry is mainly directed to the international exports and not as much to the domestic consumption); on the other hand, the Lisbon and Tagus Valley production structure is more based on services. In fact, the reason for Lisbon's advantage seems to be its higher GDP per capita.

Tables 2 and 3 depict respectively the impacts on regional income of exogenous shocks on final demand (table 2 shows $\mathbf{B_{21}}$ transposed) and the impacts on commodity output supplies (including import supplies) of the changes in the regional incomes $(\mathbf{B_{12}})^9$. It is interesting to find out that in the greater regions – Northern Region and Lisbon and Tagus Valley – the "Health and Veterinary Market Services" is the industry where a change in demand has a stronger income effect (note that that change in demand is not regionally located but can, on the contrary, occur anywhere). In Alentejo and Azores that role is assumed by "Agriculture and Hunting", while the demand for "Hotels and Restaurants" has a prominent effect on the households' income of Algarve.

Table 2 – Regional income multipliers of changes in commodity demands (transposed B_{21})

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	Northern Region	Central Region	Lisbon and T. Valley	Alentejo	Algarve	Azores	Madeira
Agriculture and hunting	0.3088	0.1881	0.3878	0.0855	0.0445	0.0373	0.0230
Forestry	0.0812	0.0714	0.1142	0.0407	0.0130	0.0031	0.0036
Fishing	0.1197	0.0616	0.1807	0.0165	0.0478	0.0215	0.0126
Coal mining and transform.	0.0473	0.0221	0.0768	0.0061	0.0084	0.0023	0.0030
Petroleum extr. and refining	0.1689	0.0751	0.2597	0.0250	0.0215	0.0087	0.0110
Electricity, gas and water	0.1128	0.0508	0.1642	0.0191	0.0127	0.0111	0.0116
Metal ores mining and transf.	0.1048	0.0495	0.1531	0.0040	0.0095	0.0041	0.0047
Non-metal. mineral pr. ext. &tr.	0.2446	0.1439	0.3320	0.0613	0.0267	0.0091	0.0147
Porcelain and pottery	0.1594	0.2278	0.2725	0.0178	0.0166	0.0070	0.0080

⁹ We have also compiled the impacts on the industry (domestic) outputs. These results can be demanded through the same E-mail mentioned in footnote 3.

Table 2 – Regional income multipliers of changes in commodity demands (transposed B_{21})

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	Northern Region	Central Region	Lisbon and T. Valley	Alentejo	Algarve	Azores	Madeira
Glass and glass prod. manuf.	0.1675	0.1925	0.2741	0.0184	0.0162	0.0075	0.0092
Other construction materials	0.1590	0.1621	0.2966	0.0231	0.0283	0.0116	0.0101
Chemical prod. manufacture	0.1188	0.0575	0.2275	0.0217	0.0138	0.0062	0.0069
Metallic products manufact.	0.1810	0.0905	0.2310	0.0151	0.0158	0.0064	0.0072
Non-electrical machinery	0.1039	0.0461	0.1374	0.0099	0.0092	0.0035	0.0041
Electrical prod. and machinery	0.1186	0.0457	0.1436	0.0123	0.0085	0.0037	0.0042
Vehicles and transport equip.	0.1019	0.0601	0.1817	0.0132	0.0109	0.0045	0.0055
Manufact. of meat products	0.2108	0.1202	0.3053	0.0460	0.0280	0.0197	0.0146
Manufact. of dairy products	0.2257	0.1347	0.3017	0.0466	0.0275	0.0261	0.0151
Manufact. of fish products	0.1308	0.0672	0.1830	0.0146	0.0280	0.0134	0.0088
Manufacture of fat products	0.1625	0.0830	0.2682	0.0315	0.0202	0.0126	0.0103
Man. of grain and legum. pr.	0.2184	0.1148	0.2808	0.0389	0.0258	0.0162	0.0140
Man. of other food products	0.1635	0.0953	0.2675	0.0360	0.0225	0.0150	0.0110
Beverages	0.1378	0.0650	0.1845	0.0187	0.0164	0.0088	0.0103
Tobacco	0.0347	0.0174	0.0639	0.0058	0.0046	0.0047	0.0033
Textiles and textile products	0.2950	0.0894	0.1923	0.0199	0.0156	0.0077	0.0085
Leather and leather products	0.2454	0.0527	0.1714	0.0146	0.0132	0.0059	0.0066
Wood and cork products	0.2471	0.1017	0.2324	0.0281	0.0193	0.0073	0.0093
Pulp, paper, publ. and printing	0.1612	0.0946	0.2702	0.0214	0.0172	0.0074	0.0092
Rubber and plastic products	0.1561	0.0739	0.1826	0.0145	0.0128	0.0055	0.0066
Other manufactured products	0.1724	0.0586	0.1951	0.0144	0.0137	0.0057	0.0069
Construction	0.2250	0.1139	0.3028	0.0246	0.0267	0.0129	0.0159
Recycling and repair services	0.2251	0.1096	0.3899	0.0306	0.0305	0.0117	0.0128
Wholesale and retail trade	0.2559	0.1163	0.4007	0.0333	0.0333	0.0134	0.0168
Hotels and restaurants	0.1836	0.0980	0.3069	0.0336	0.0606	0.0146	0.0271
Land transport and pipelines	0.2458	0.1347	0.4039	0.0380	0.0379	0.0146	0.0174
Water and air transp. serv.	0.1337	0.0514	0.3010	0.0174	0.0252	0.0192	0.0615
Supporting aux. transp. ser.	0.1624	0.0643	0.3422	0.0276	0.0332	0.0134	0.0248
Communication services	0.1498	0.0741	0.2349	0.0244	0.0217	0.0094	0.0114
Banking and financial serv.	0.1729	0.0696	0.3428	0.0218	0.0206	0.0113	0.0105
Insurances	0.2729	0.1410		0.0383	0.0428	0.0200	0.0176
Housing services	0.4968	0.2609	0.6138	0.0638	0.0787	0.0295	0.0365
Business services	0.1211	0.0526	0.3145	0.0169	0.0213	0.0073	0.0085
Educat. and res. market serv.	0.1908	0.0862	0.2788	0.0246	0.0198	0.0116	0.0176
Health and vet. market servic.	0.5000	0.2471	0.7748	0.0501	0.0502	0.0220	0.0273
Other market services	0.2163	0.0964	0.4043	0.0341	0.0328	0.0153	0.0175
Public adm. non-market serv.	0.2921	0.1584	0.5301	0.0609	0.0429	0.0314	0.0360
Edu. and res. non-mark. serv.	0.4265	0.2201	0.5077	0.0713	0.0510	0.0294	0.0273
Health and v. non-market ser.	0.3426	0.1768		0.0388	0.0343	0.0299	0.0325
Other non-market services	0.3698	0.1762	0.4770	0.0562	0.0419	0.0258	0.0305

Hotels and restaurants

Land transport and pipelines

Water and air transp. serv.

Communication services

Supporting aux. transp. ser.

Banking and financial serv.





Table 3 – Commodity output multipliers of changes in regional incomes (B ₁₂)								
	Northern Region	Central Region	Lisbon and T. Valley	Alentejo	Algarve	Azores	Madeira	
Agriculture and hunting	0.1465	0.1297	0.1405	0.1337	0.1371	0.1444	0.1280	
Forestry	0.0118	0.0102	0.0091	0.0071	0.0085	0.0081	0.0069	
Fishing	0.0220	0.0192	0.0284	0.0226	0.0360	0.0250	0.0182	
Coal mining and transform.	0.0033	0.0030	0.0036	0.0034	0.0035	0.0035	0.0036	
Petroleum extr. and refining	0.0975	0.0905	0.0992	0.0971	0.1025	0.0750	0.0883	
Electricity, gas and water	0.0917	0.0845	0.1004	0.0949	0.0980	0.0976	0.1020	
Metal ores mining and transf.	0.0096	0.0092	0.0094	0.0086	0.0096	0.0086	0.0074	
Non-metal. mineral pr. ext. &tr.	0.0019	0.0019	0.0019	0.0017	0.0021	0.0019	0.0017	
Porcelain and pottery	0.0021	0.0022	0.0024	0.0016	0.0016	0.0020	0.0028	
Glass and glass prod. manuf.	0.0038	0.0031	0.0035	0.0032	0.0037	0.0034	0.0031	
Other construction materials	0.0023	0.0023	0.0022	0.0020	0.0028	0.0023	0.0021	
Chemical prod. manufacture	0.0849	0.0762	0.0890	0.0862	0.0920	0.0906	0.0724	
Metallic products manufact.	0.0145	0.0138	0.0142	0.0134	0.0153	0.0146	0.0127	
Non-electrical machinery	0.0104	0.0099	0.0098	0.0087	0.0097	0.0092	0.0078	
Electrical prod. and machinery	0.0291	0.0277	0.0306	0.0259	0.0284	0.0295	0.0233	
Vehicles and transport equip.	0.0789	0.0779	0.0736	0.0681	0.0703	0.0562	0.0459	
Manufact. of meat products	0.0803	0.0736	0.0813	0.0723	0.0768	0.0756	0.0658	
Manufact. of dairy products	0.0307	0.0289	0.0345	0.0334	0.0325	0.0419	0.0306	
Manufact. of fish products	0.0228	0.0193	0.0215	0.0175	0.0159	0.0163	0.0101	
Manufacture of fat products	0.0141	0.0140	0.0134	0.0153	0.0147	0.0108	0.0101	
Man. of grain and legum. pr.	0.0474	0.0426	0.0440	0.0486	0.0456	0.0528	0.0497	
Man. of other food products	0.0451	0.0389	0.0467	0.0439	0.0448	0.0542	0.0404	
Beverages	0.0209	0.0164	0.0204	0.0187	0.0231	0.0173	0.0152	
Tobacco	0.0175	0.0113	0.0180	0.0186	0.0186	0.0222	0.0172	
Textiles and textile products	0.0916	0.0812	0.0918	0.0848	0.0896	0.0809	0.0853	
Leather and leather products	0.0242	0.0216	0.0236	0.0246	0.0245	0.0228	0.0293	
Wood and cork products	0.0276	0.0272	0.0324	0.0215	0.0282	0.0286	0.0215	
Pulp, paper, publ. and printing	0.0331	0.0317	0.0360	0.0305	0.0353	0.0315	0.0330	
Rubber and plastic products	0.0181	0.0204	0.0194	0.0184	0.0205	0.0196	0.0159	
Other manufactured products	0.0173	0.0159	0.0168	0.0146	0.0170	0.0170	0.0142	
Construction	0.0174	0.0178	0.0163	0.0154	0.0217	0.0175	0.0160	
Recycling and repair services	0.0862	0.0781	0.0789	0.0732	0.0793	0.0604	0.0634	
Wholesale and retail trade	0.1812	0.1656	0.1824	0.1707	0.1830	0.1651	0.1543	

0.1209

0.0228

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0.0875

0.0289

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0.0140

0.0355

0.0040

Table 3 – Commodity output multipliers of changes in re	gional incomes (B)



	The second				and the same		
	Northern Region	Central Region	Lisbon and T. Valley	Alentejo	Algarve	Azores	Madeira
Insurances	0.0087	0.0074	0.0085	0.0070	0.0083	0.0069	0.0066
Housing services	0.0789	0.0874	0.0683	0.0708	0.1081	0.0823	0.0752
Business services	0.0606	0.0556	0.0634	0.0545	0.0634	0.0538	0.0522
Educat. and res. market serv.	0.0200	0.0172	0.0254	0.0158	0.0185	0.0134	0.0165
Health and vet. market servic.	0.0320	0.0295	0.0319	0.0226	0.0396	0.0267	0.0251
Other market services	0.0339	0.0263	0.0318	0.0282	0.0354	0.0248	0.0261
Public adm. non-market serv.	0.0011	0.0013	0.0014	0.0014	0.0014	0.0009	0.0012
Edu. and res. non-mark. serv.	0.0006	0.0005	0.0008	0.0004	0.0005	0.0004	0.0005
Health and v. non-market ser.	0.0006	0.0005	0.0006	0.0004	0.0007	0.0004	0.0004
Other non-market services	0.0155	0.0159	0.0149	0.0185	0.0190	0.0121	0.0164

ANNEX

The matrix inversion procedure

Let **q** be the vector of commodity outputs – or commodity supplies since imports are included – and **g** be the vector of industry outputs (in fact, those outputs only fill 49 of the 56 entries of those vectors; the last 7 entries, which comprise the total incomes of the households residing in the 7 Portuguese regions, are the same in both vectors). In the main text of this paper we assumed that the technical coefficients matrix **A*** is computed by dividing the entries of **A** by the outputs of **q**. However, these technical relationships shall be settled instead at industry level, because the same commodity can be produced by a different technology in a different industry. That means that the basic input-output equation that we took as a starting point in this paper is really:

(7)
$$q = A^* g + e$$

instead of (3') in the main text, where ${\bf e}$ is the final demand vector. However, the output vectors ${\bf q}$ and ${\bf q}$ can be related as follows:

(8)
$$q = g - tr_1 + tr_2 + im + tm + t$$

in which tr_1 and tr_2 are by-products and incidental sales of commodities that are transferred from the industry where they actually are produced (and then subtracted by tr_1) to the commodity group where they belong by their very nature (and then added by tr_2). tr_2 im is the vector of imports (including taxes on imports), tr_2 are the trade margins and tr_2 means the VAT. Note that in the Portuguese National Accounts, and therefore in our RAM as well, tr_1 and tr_2 only record residual flows: the main share of secondary production is already included in the industry where it belongs by its nature. On the other hand t only bears non-deductible VAT that falls upon the private consumption. Although the outputs are evaluated at purchasers' prices, we have excluded other non-deductible VAT from the sales to intermediate consumption and to GFCF, and then from the value of the total output of each commodity (however, it is assumed to be a cost and then included in the total value of the output of the industry that buys the commodities).



We assumed that:

$$tr_1 = \hat{Z}_1g$$
 and $tr_2 = z_2i'tr_1 = z_2i'\hat{Z}_1g$

where $\hat{\mathbf{Z}}_1$ is a diagonal matrix and \mathbf{z}_2 a vector of coefficients; i' is a row-vector fulfilled with 1s. By-products and incidental sales are supposed to depend on the output of the industries where they are generated (\mathbf{tr}_1 depends on \mathbf{g}), while their structure by commodities is deemed to be invariant, i. e. \mathbf{tr}_2 depends on the total entries of \mathbf{tr}_1 .

Imports and trade margins are supposed to be fixed shares of the commodity outputs (VAT excluded):

$$im = \hat{Z}_3(q-t)$$
 and $tm = \hat{Z}_4(q-t)$

VAT is assumed to depend on households' consumption, which is a function of their total income

$$t = \hat{Z}_5 c = \hat{Z}_5 A^* \hat{J} q$$

where \mathbf{c} is the vector of the households' consumption, \mathbf{A}^{\star} is the technical coefficients matrix and $\hat{\mathbf{J}}$ is a square matrix with 1s in the last 7 entries of the main diagonal and 0s elsewhere ($\hat{\mathbf{J}}\mathbf{q}$ is a vector of 0s, except in its last 7 entries, which are the households' incomes).

Doing

$$q - t = (I - \hat{Z}_5 A^* \hat{J}) q = W q$$

we can write

$$im = \hat{Z}_3 W q$$
 and $tm = \hat{Z}_4 W q$

Those equations can now be inserted into (8), getting:

q - t = W q = g -
$$\hat{Z}_1$$
 g + z_2 i' \hat{Z}_1 g + \hat{Z}_3 W q + \hat{Z}_4 W q

$$(I - \hat{Z}_3 - \hat{Z}_4) W q = (I - \hat{Z}_1 + z_2 i' \hat{Z}_1) g$$
(8') g = $(I - \hat{Z}_1 + z_2 i' \hat{Z}_1)^{-1} (I - \hat{Z}_3 - \hat{Z}_4) W q = H W q$

On the other hand, rewriting equation (7) we have:

(7')
$$q = A^* g + Z_a (q - t) + e = A^* g + Z_a W q + e$$

The reason why we added up $\mathbf{Z_4}$ ($\mathbf{q}-\mathbf{t}$) above is that the technical coefficients matrix \mathbf{A}^* has its 33rd row, concerning the retail and wholesale trade, entirely fulfilled with 0s; instead, the trade output matches the trade margins (the difference between the matrices $\mathbf{\hat{Z}_1}$ and $\mathbf{Z_4}$ is that the

former is a diagonal matrix while the latter has the same coefficients on its $33^{\rm rd}$ row, and 0s elsewhere).



Thus, from the substitution of (8') into (7') we find:

$$q = A^* H W q + Z_4 W q + e$$

$$q = (I - A^* H W - Z_4 W)^{-1} e$$

and

$$g = H W (I - A^* H W - Z_4 W)^{-1} e$$

The inverse matrix **B** that is discussed in the main text of this paper is in fact:

$$(I - A^* H W - Z_4 W)^{-1}$$
 or $H W (I - A^* H W - Z_4 W)^{-1}$

depending on whether we are computing impacts on commodity or industry outputs. The impacts on households' income (i. e. the multipliers ${\bf B_{21}}$ and ${\bf B_{22}}$) are the same in both matrices.

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